

Yunnan/Beijing 2019

Stellar Atmospheres

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Planetarium

2. The Line Profile

Programme

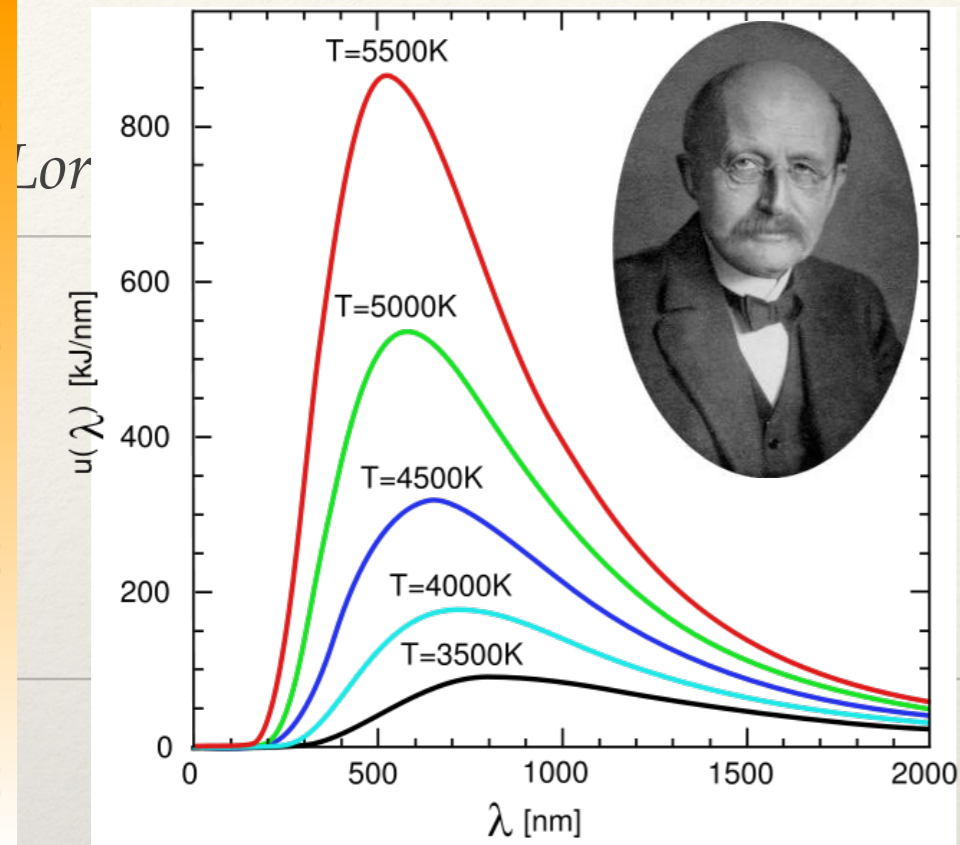
1. The Model Atmosphere

2. The Line Profile

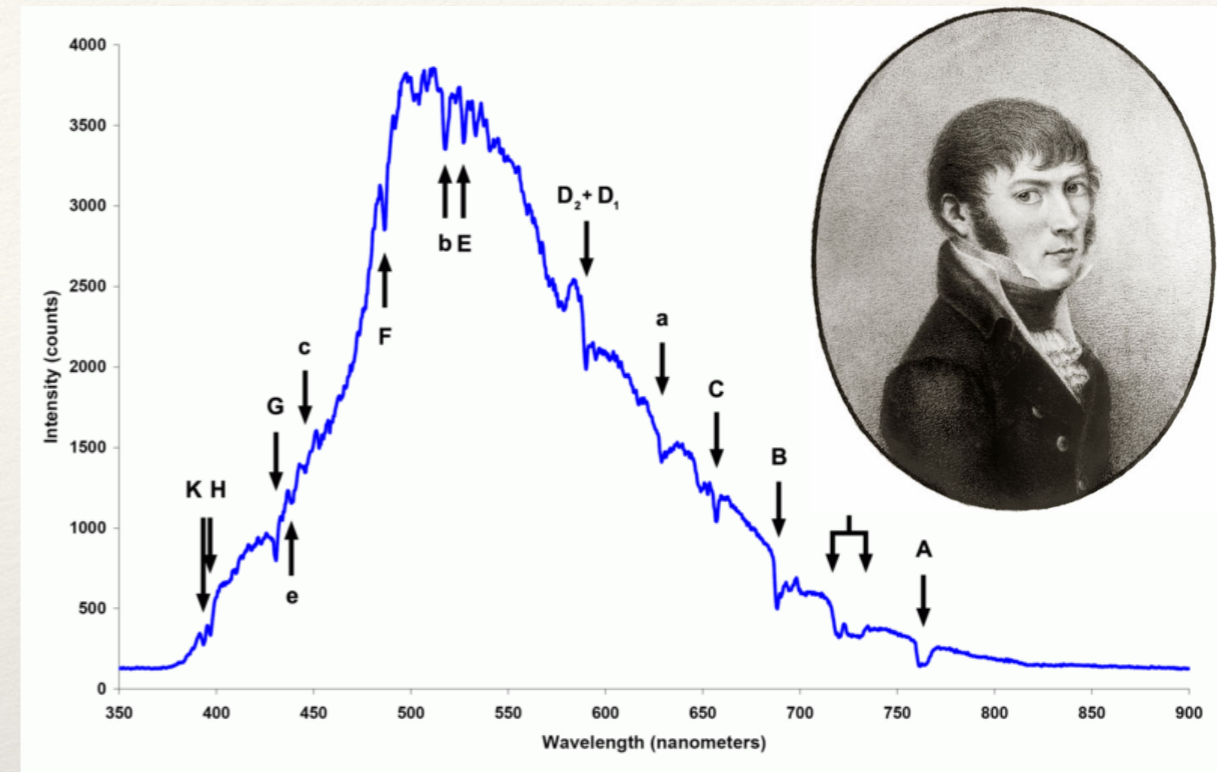
3. Spectral Analysis

Stellar Atmospheres

1894: Max Planck



1814: Joseph von Fraunhofer



Stellar interior: radiation in full LTE is “grey”: obeys Planck’s law

Stellar surface: radiation obeys Kirchoff’s laws

Absorption lines governed by number of ions and density of electrons

A “model atmosphere” allows the emergent radiation to be compared with the observed spectrum.

.1. Spectral Diagnostics

Total flux
distribution

T_{eff} : effective
temperature

E_{B-V} : extinction

θ : angular
radius

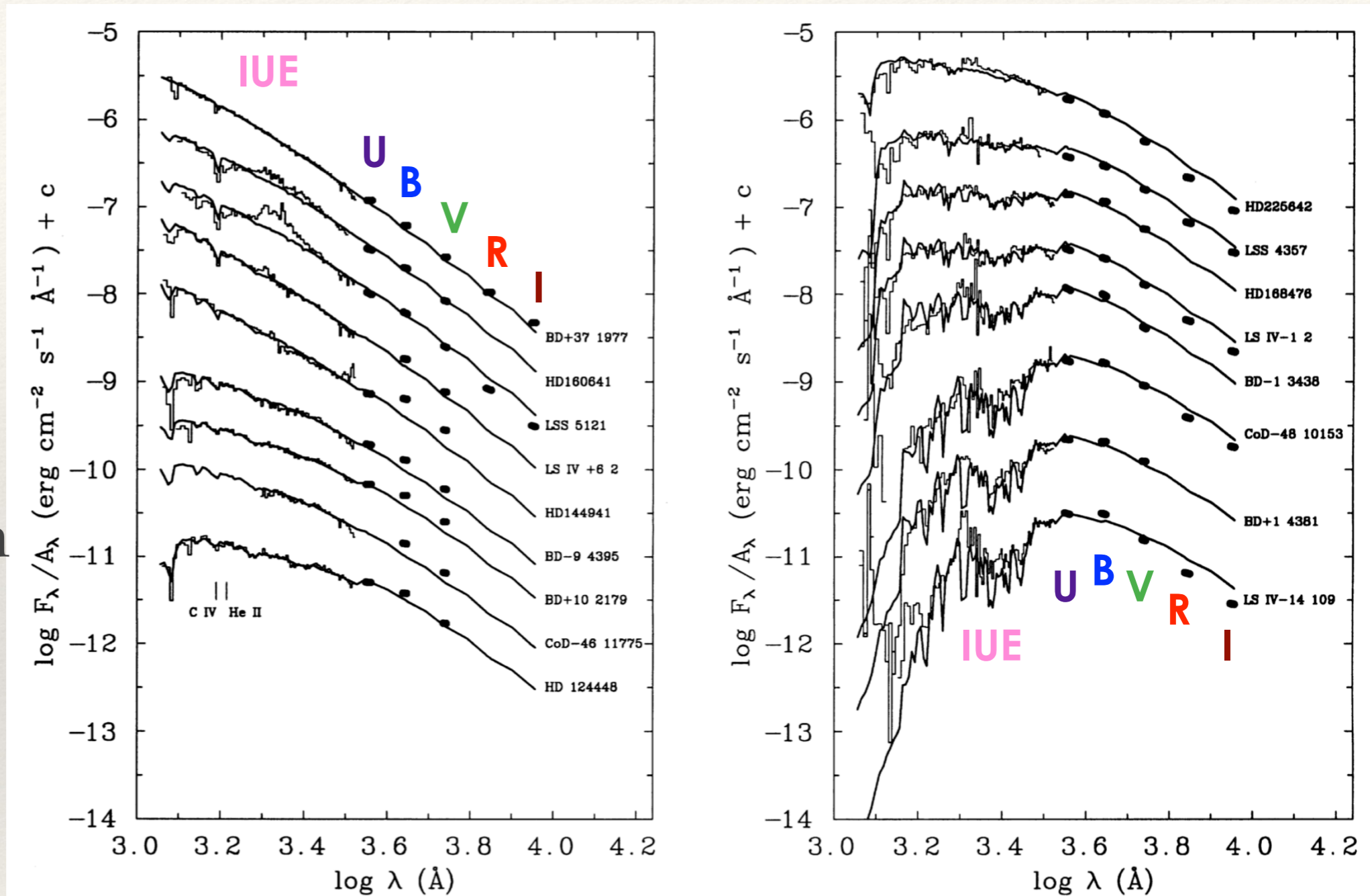


Figure 2. One SW/LW pair of *IUE* spectra for each programme star, binned to the resolution of the model atmosphere grid (thin histogram), together with the photometry from Table 3 (solid points), is compared with the theoretical flux distributions (thick curve) that best fit the *IUE* spectra. The spectra have been dereddened by the amount shown in Table 4 and multiplied by an arbitrary constant. The *IUE* and model spectra correspond to the last entry for each star in Tables 1 and 4.

.1. Spectral Diagnostics

Major absorption lines

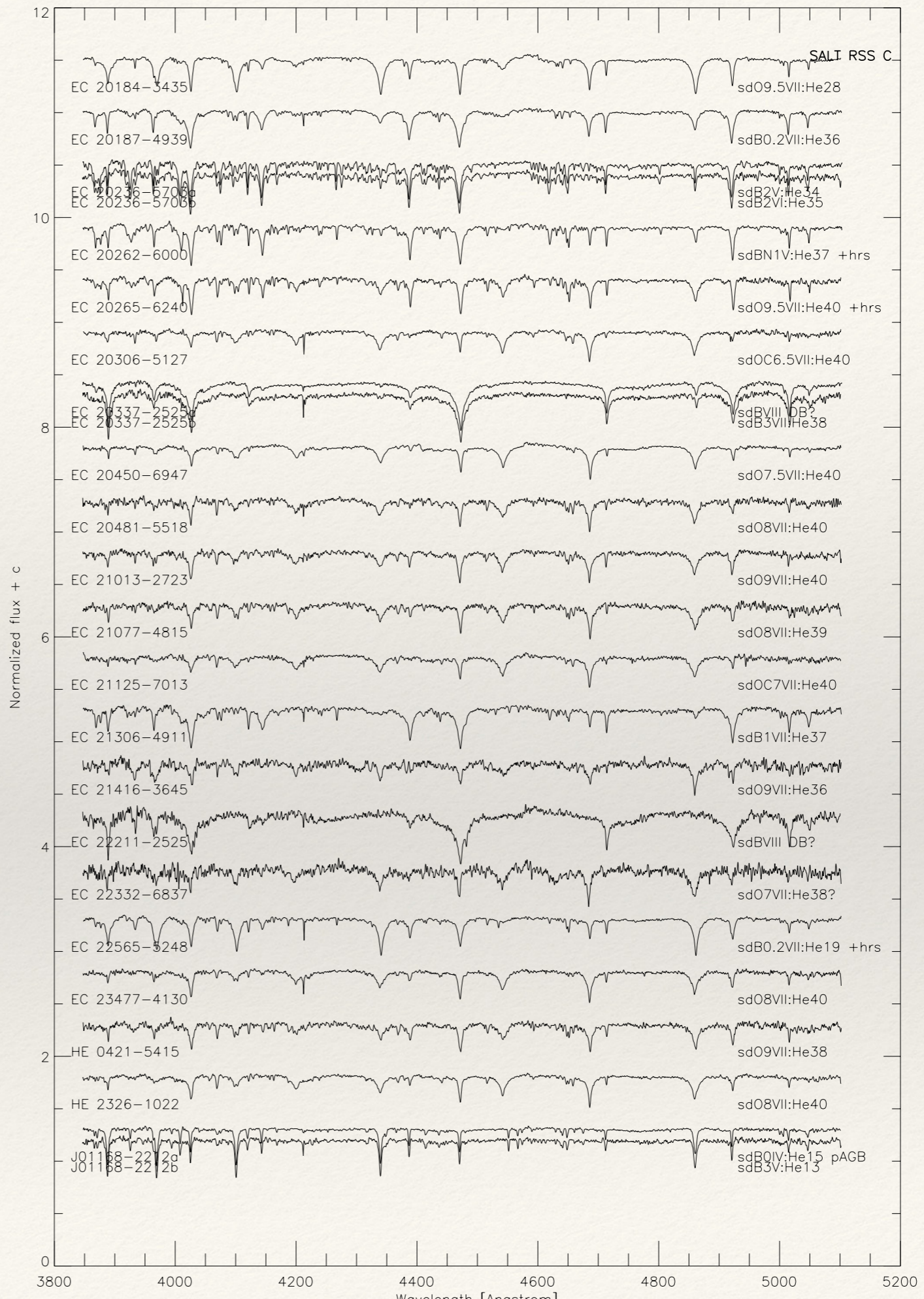
T_{eff} : effective temperature

g : surface gravity

$[\text{He}/\text{H}]$: helium / hydrogen ratio

$[\text{Fe}/\text{H}]$: metallicity

v_{rad} : radial velocity



.1. Spectral Diagnostics

Major absorption lines

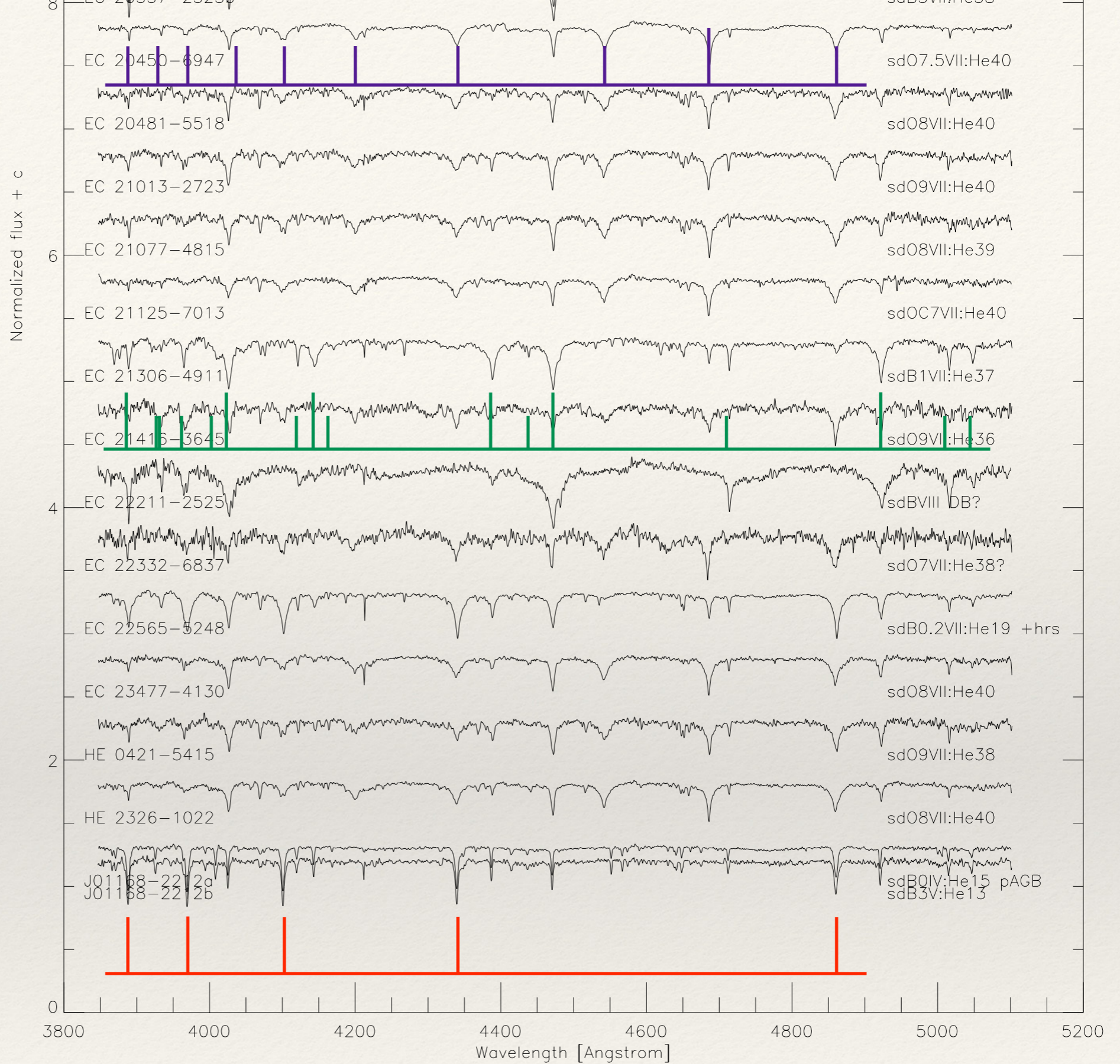
T_{eff} : effective temperature

g : surface gravity

$[\text{He}/\text{H}]$: helium / hydrogen ratio

$[\text{Fe}/\text{H}]$: metallicity

v_{rad} : radial velocity



.1. Spectral Diagnostics

High-resolution spectrum

T_{eff} : effective temperature

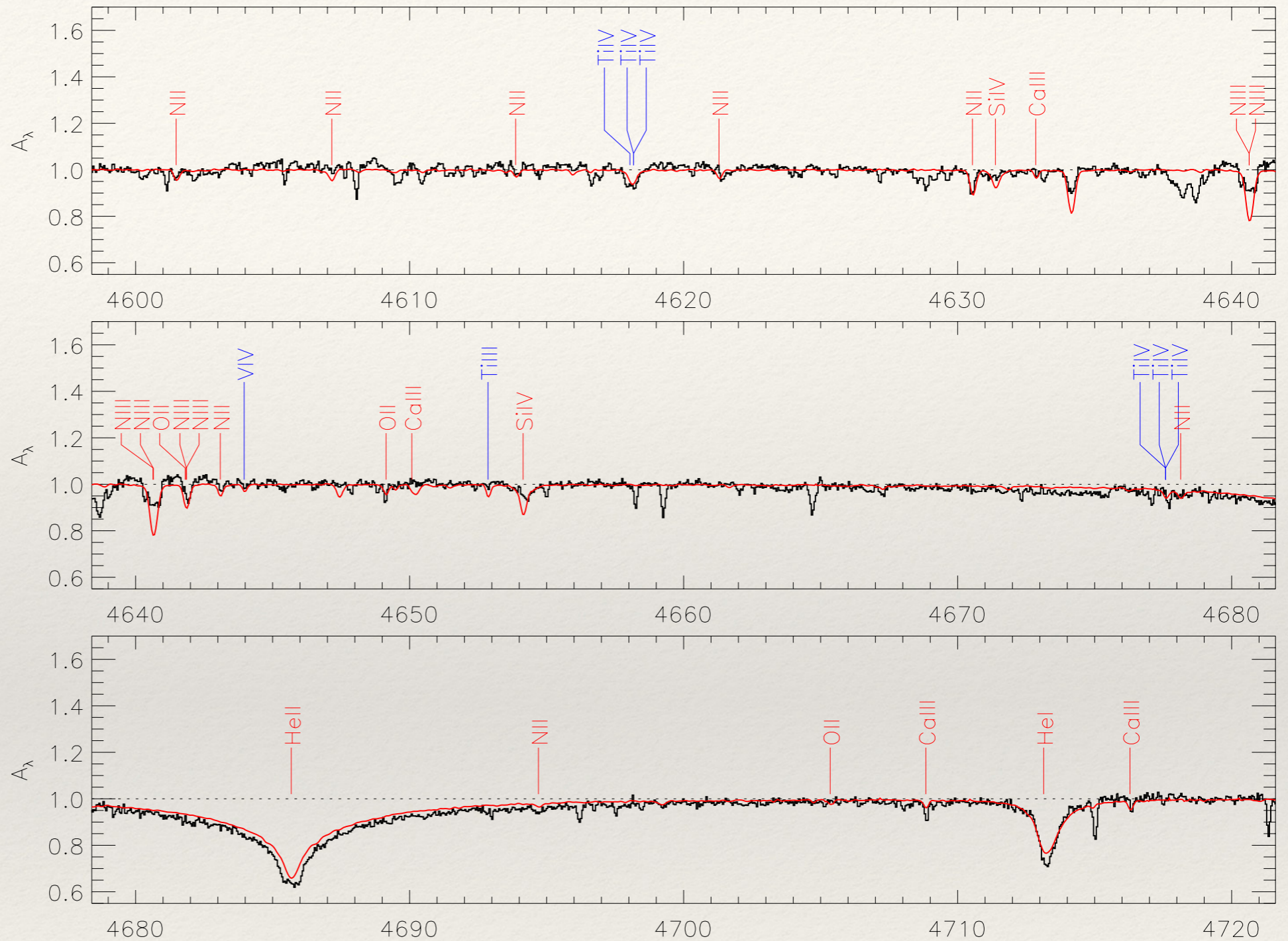
g : surface gravity

n_i : elemental abundances

v_{turb} : microturbulent velocity

$v_{\text{rot}} \sin i$: projected rotation velocity

v_{rad} : radial velocity



.2. Equivalent widths

The line profile

Equivalent widths

Abundances from W_λ

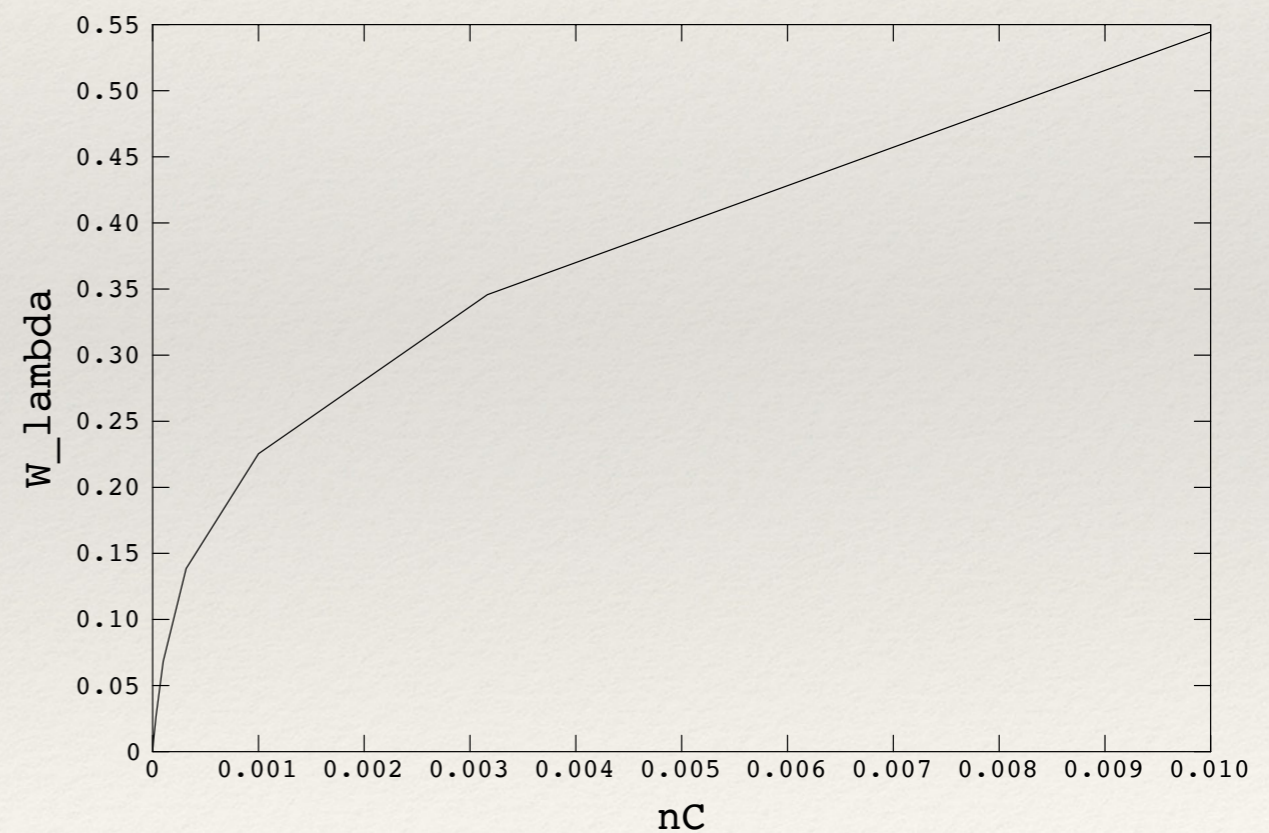
Computing the line profile

Spectrum synthesis

Atomic Data

$$A_\lambda = (1 - F_\lambda / F_{\text{continuum}})$$

$$W_\lambda = \int A_\lambda d\lambda$$



.3. The line profile: I

$$A_\nu = (1 - F_\nu / F_c)$$

Pure LTE (no scattering)

$$S_\nu = B_\nu$$

$$F_\nu = \int_{s_1}^{s_2} S_\nu E_2(\tau_\nu) d\tau_\nu$$

$$\tau_\nu = \int_{s_1}^s \kappa_\nu(s) ds$$

For F_c : $\kappa_\nu = \kappa_c$

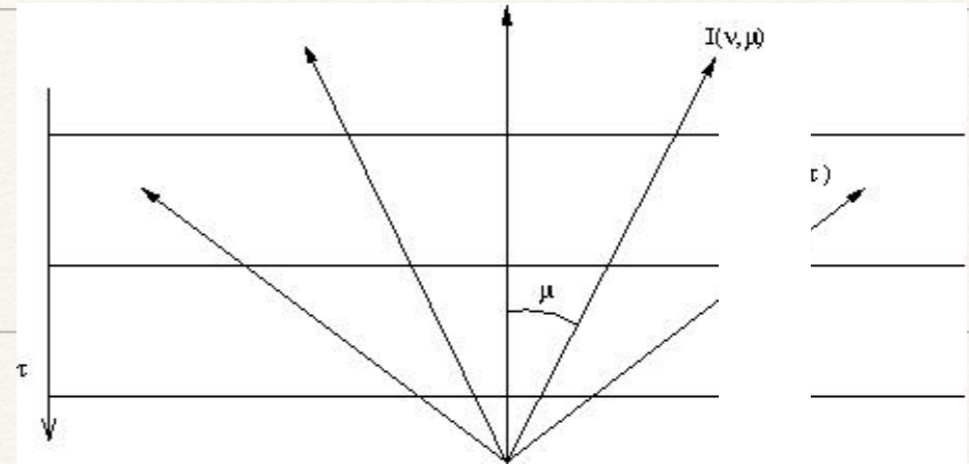
For F_ν : $\kappa_\nu = \kappa_c + \chi I \phi_\nu$

Cheap and cheerful !

HOWEVER:

Scattering cannot be ignored
at high temperatures and /
or low-gravities.

.3. The line profile: II



$$\mu = \cos \theta$$

$$A_\nu = (1 - F_\nu / F_c)$$

$$F_\nu = 2 \int_0^1 I_{\nu\mu} \mu d\mu$$

$$I_{\nu\mu} = \int_0^\infty S_{\tau\nu} e^{-\tau/\mu} d\tau$$

Semi-LTE: including e- scattering

$$\tau_\nu = \int_{s_1}^{s_2} \kappa_\nu(s) ds$$

$$S_\nu = (\kappa_\nu B_\nu + \sigma_\nu J_\nu) / (\kappa_\nu + \sigma_\nu)$$

$$J_\nu = (4\pi)^{-1} \oint I_\nu d\Omega$$

$$S_c : \kappa_\nu = \kappa_c$$

$$S_\nu : \kappa_\nu = \kappa_c + \chi I \phi_\nu$$

$$\mu \frac{dI_\nu}{d\tau_\nu} = I_\nu - S_\nu$$

MUST solve transfer equation explicitly

.3. The line profile: III

Doppler broadening (thermal, microturbulence):

$$\Delta\nu_D = \lambda \sqrt{C_T T / A_k + C_v v_t^2}$$

Radiative broadening: Γ_r

Electron (Stark) broadening: Γ_e

Ion (van der Waal's) broadening - heavy ions : Γ_W

⇒ Voigt profile:

$H(a, \nu)$:

$$a = \frac{(\Gamma_r + n_e \Gamma_e + n_H \Gamma_W)}{4\pi \Delta\nu_D}$$

$$\nu = \Delta\nu / \Delta\nu_D$$

⇒ line absorption coefficient:

$$\chi_l \phi_\nu = n_{ijk} f_l H(a, \nu) / \Delta\nu_D$$

Pressure broadening (quadratic Stark effect) - H, He, resonance lines

.3. The line profile: IV

Temperature: lines from adjacent ions. *e.g. C⁺ and C⁺⁺*

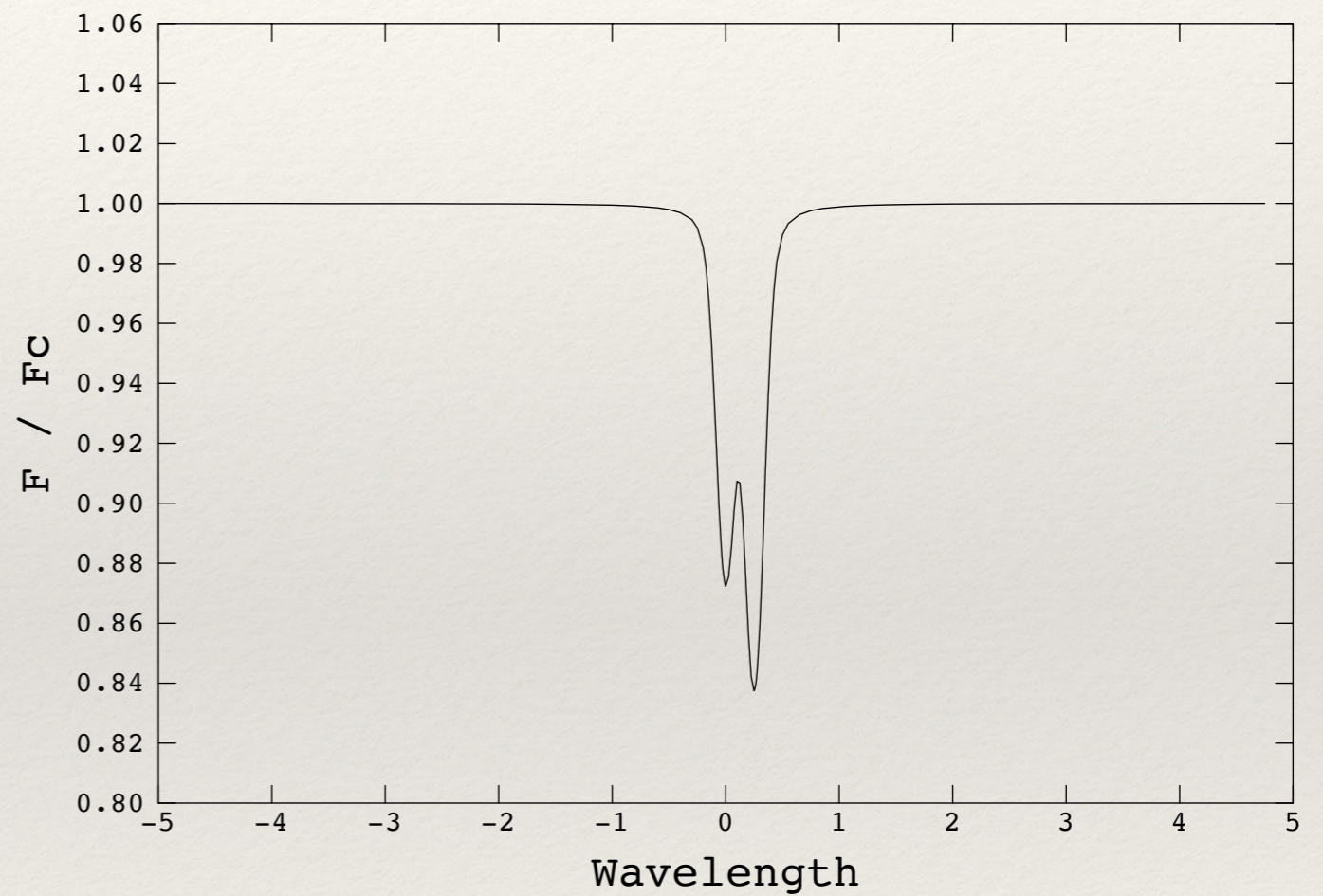
Pressure: lines with strong wings. *e.g. H, He*

Abundance: weak lines

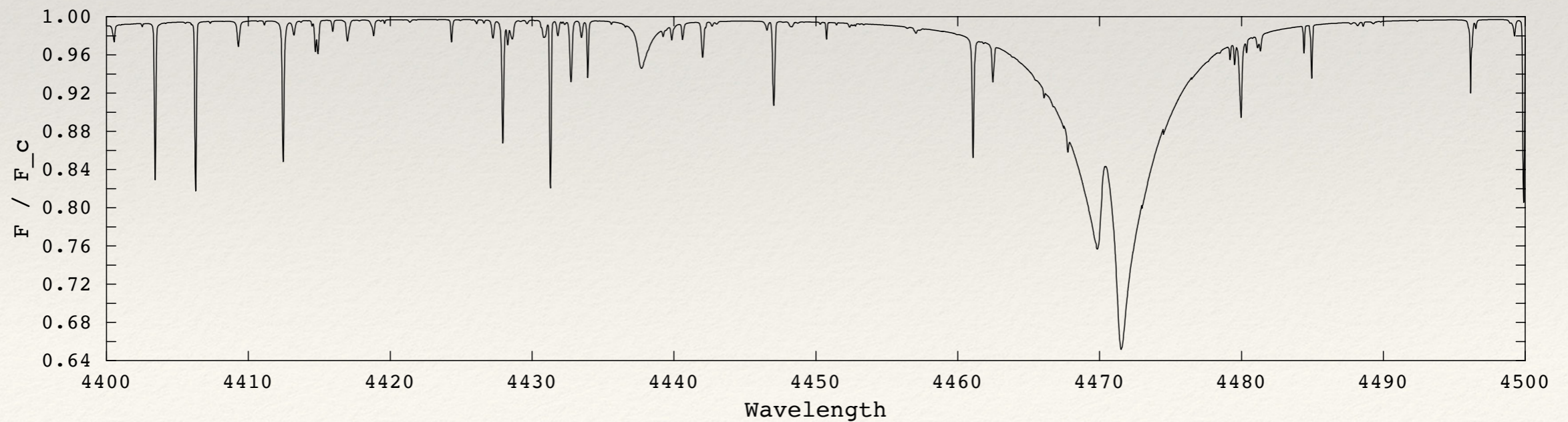
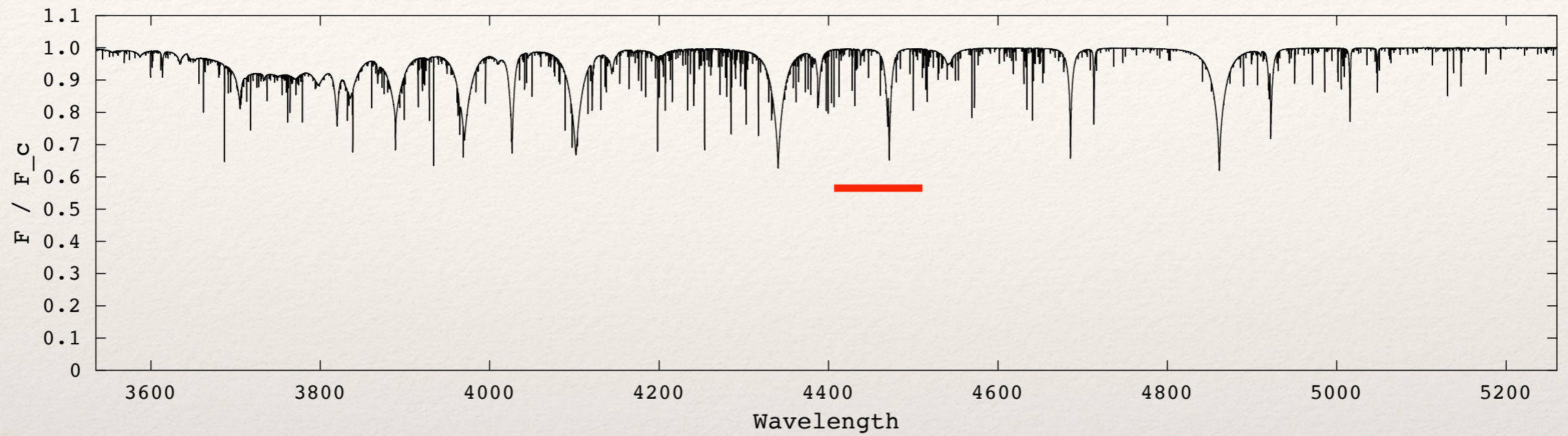
Turbulence: sharp lines. *e.g. from heavy ions: Fe⁺⁺*

.4. Examples: I - an isolated line

❖ C II 4267



.4. Examples: II - spectrum synthesis



.5. Atomic Data

For every line:

Z : atomic number

I : ionisation stage

λ : wavelength

gf : transition probability \times
statistical weight

χ_{ijk} : excitation potential of
lower level

Γ_r : radiative damping constant

Γ_e : electron damping constant

Γ_w : ion damping constant

For strong lines:

Pressure broadening
coefficients / profiles

H: Vidal, Cooper & Shamey:

Lyman, Balmer, Paschen

HeI: Beauchamp et al. (optical),

Barnard et al.

(4471,4026,4921,4388),

Dimitrijevic (various),

HeII: Schöning & Butler

Metals: lte_lines

.6. Computational Tools: types

1. Model atmospheres
2. Formal solutions (emergent spectrum, lines, ...)
3. Atomic data
4. Interface — theory / observation — analysis
5. Other resources

.6. Computational Tools: codes

1. Model atmosphere (structure important, spectrum approximate, photometry)

1. ATLAS (Kurucz), MARCS (Gustaffson), **STERNE (Jeffery+)**, ...

2. PHOENIX, TLUSTY (Hubeny), TMAP (Werner)

3. CMFGEN (Hillier, Crowther), PoWR (Hamann)

2. Formal solution (structure assumed, spectrum crucial)

1. SYNTHÉ (Kurucz), **SPECTRUM (Jeffery)**, SPECTRUM (Gray), LINFOR, MOOG (Snedden), SME (Valenti+Piskunov), ...

2. PHOENIX, SYNSPEC, TMAP

3. Atomic data

1. Kurucz, Tübingen, VALD, NIST, OP, Iron Project, ...

lte-codes

Armagh Stellar Atmospheres Software Collection

http://193.63.77.2:2805/~SJeffery/software_store/index.html

- `sterne` - model atmospheres
- `spectrum` - formal solutions
- `ffit` - optimization to fluxes
- `sfit` - optimization to spectra
- `lte_lines` - atomic data
- `idlines` - line identification and fit verification
- [`isfit` - interactive spectral fitting]

C.S.Jeffery, N.T.Behara, C.Winter

Armagh Stellar Atmosphere Software
A Guide and Reference Manual

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DRAFT - October 28, 2019

https://armaghop.sharepoint.com/sites/SJeffery/lte_codes/

.7. Spectral Analysis - next time

1. Spectral classification
2. Spectral energy distribution (SED) fitting
3. Coarse analysis (for T_{eff} , $\log g$)
4. Fine analysis (for abundances)
5. Automatic methods (χ^2 , ANN, PCA, GA, ...)
6. Errors